

Probing the security landscape for authenticated key establishment protocols

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Security Models in Cryptography

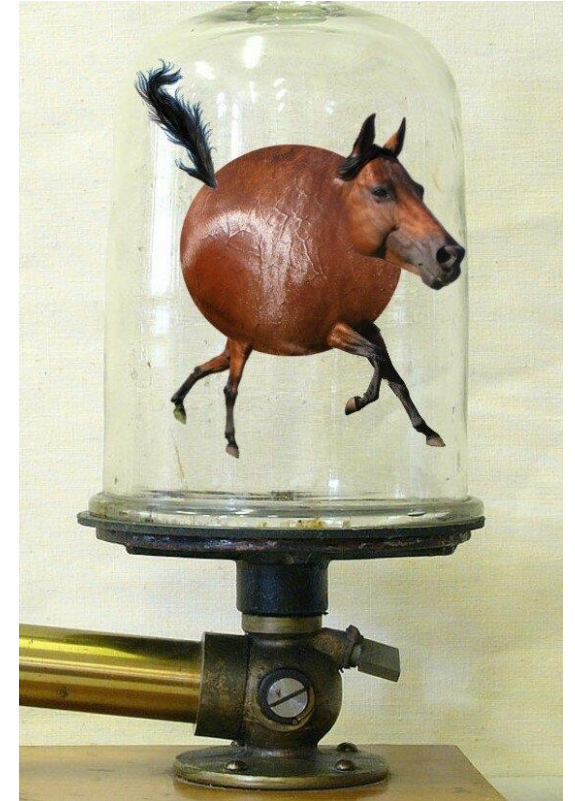
Cryptanalysis steps:

- 1) Identify a relevant security model
- 2) Describe the model formally
- 3) Get security estimation within a formal model

Step 1 is based on expert experience

Phong Q. Nguyen:

«There are a lot of similarities between cryptology and physics. Both use a lot of mathematics, but neither is part of mathematics.»



Security Models in Cryptography

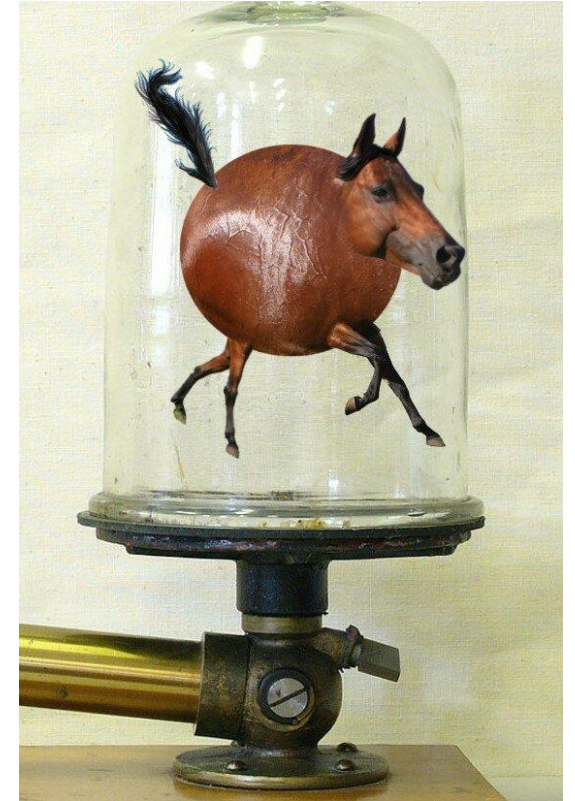
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Threats and Adversary Capabilities

Security model:

- Threats *what the adversary wants*
- Adversary capabilities *what the adversary can*
- Adversary resources quantitative characteristics of the adversary capabilities

Security landscape for cryptosystem is a set of possible security models.

We propose 7 steps to systematically form security landscape.

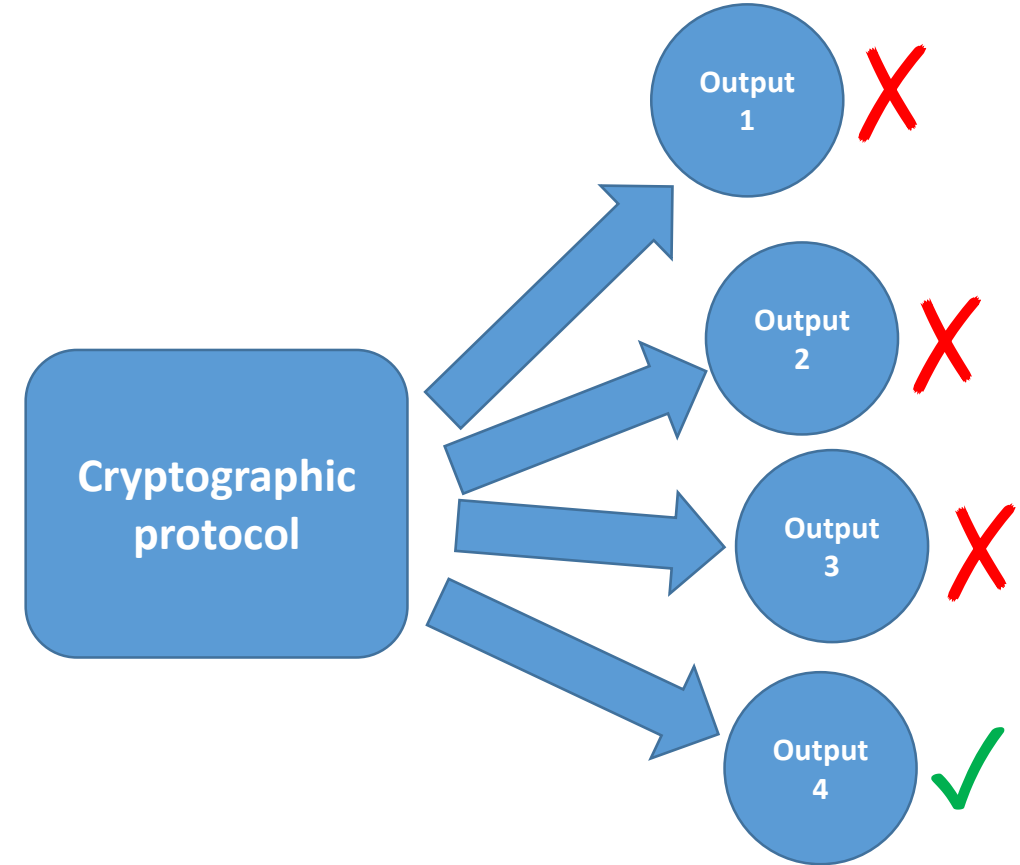
Step 1. Define the interface



Security Landscape

Step 1. Define the interface

Step 2. Determine “(ab)normal” outputs

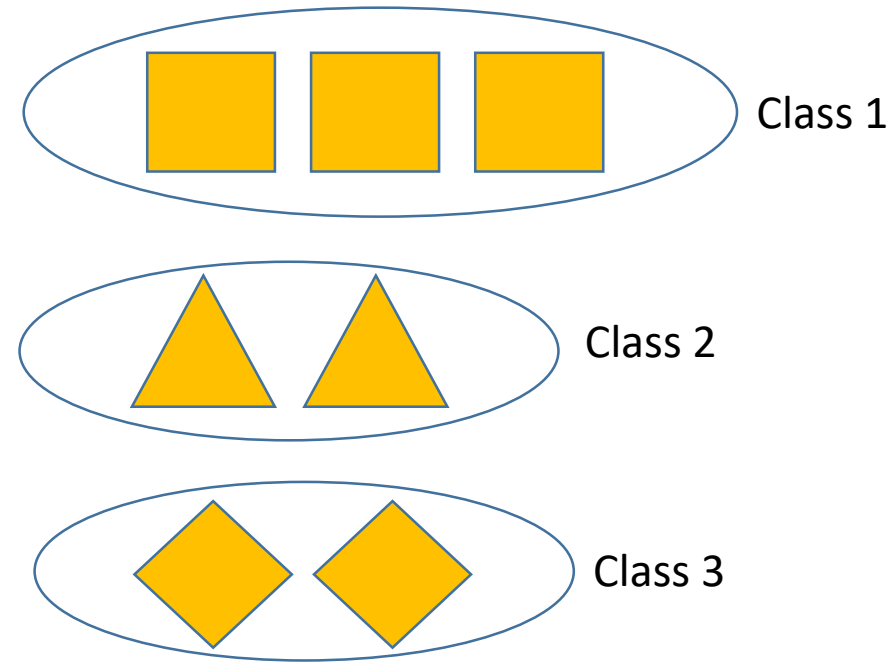


Security Landscape

Step 1. Define the interface

Step 2. Determine “(ab)normal” outputs

Step 3. List (systematically) adversary capabilities



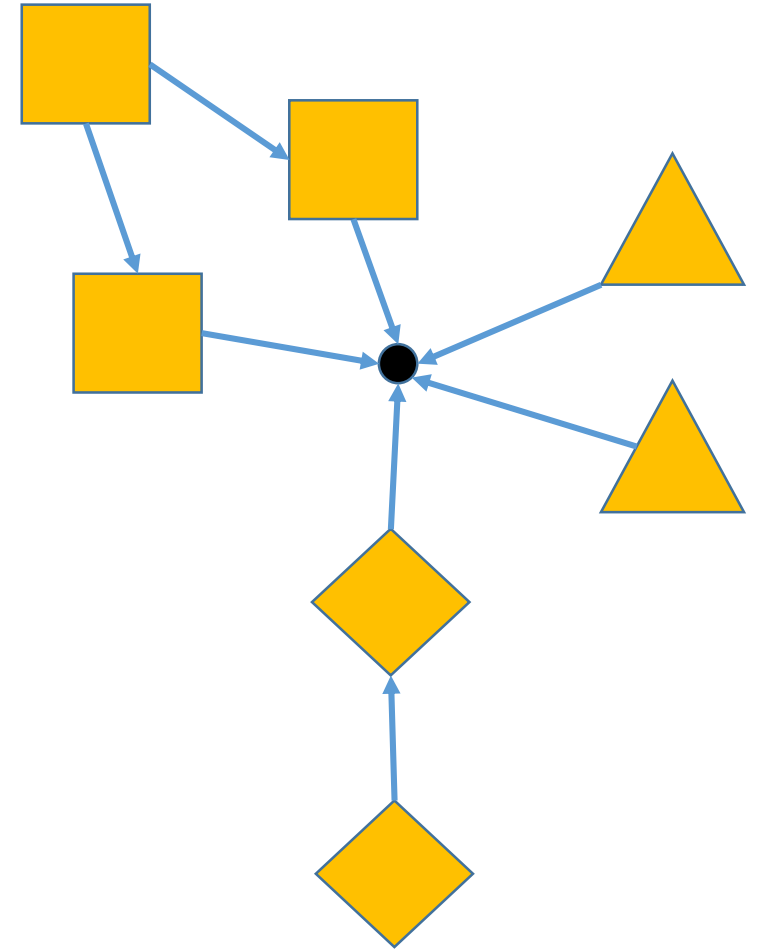
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Step 1. Define the interface

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Step 4. Identify the interdependencies of capabilities



Security Landscape

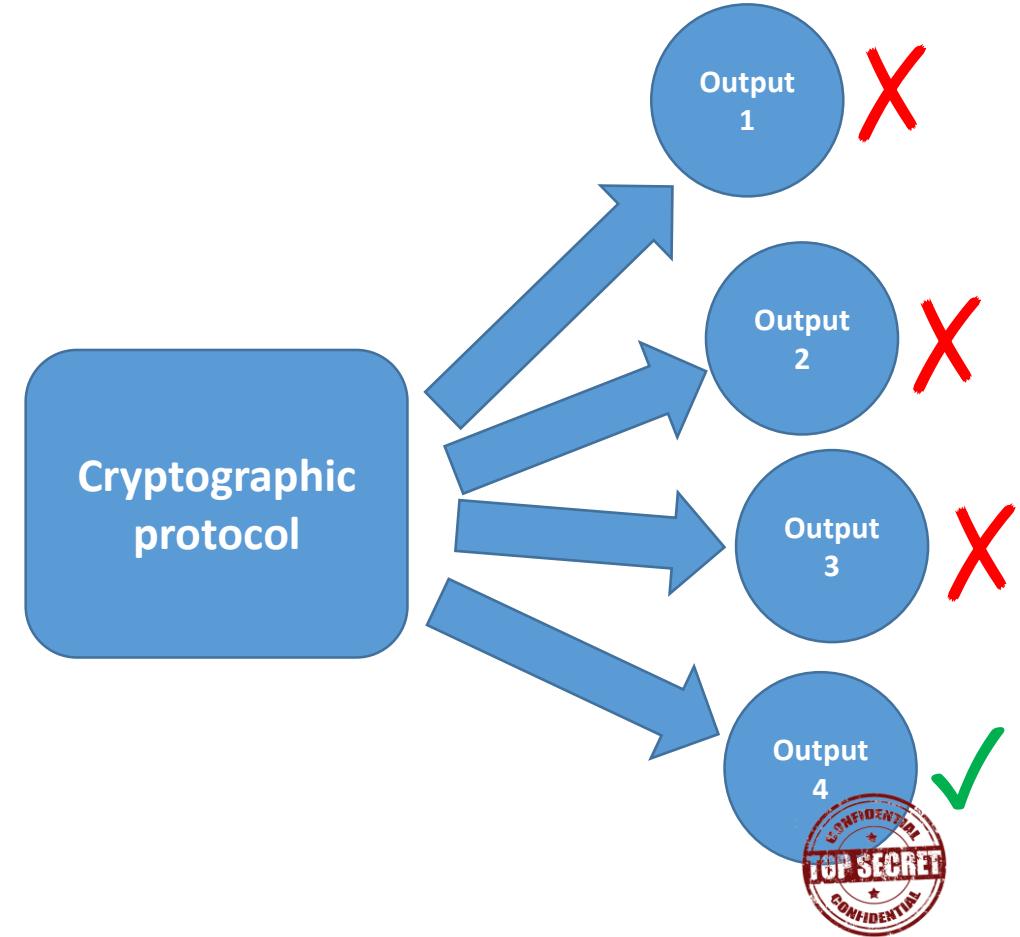
Step 1. Define the interface

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Step 5. List (systematically) confidential information



Security Landscape

Step 1. Define the interface

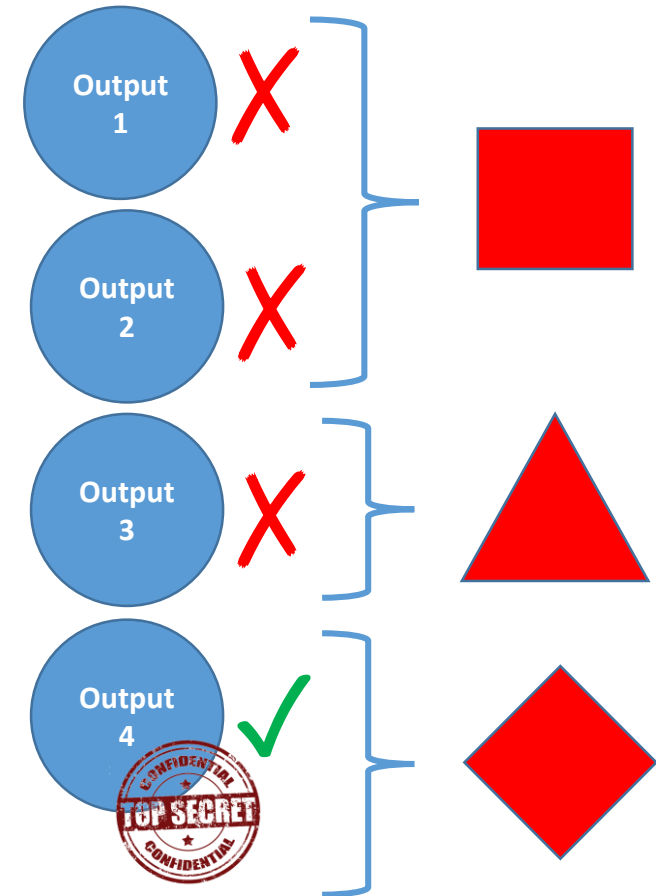
Step 2. Determine “(ab)normal” outputs

Step 3. List (systematically) adversary capabilities

Step 4. Identify the interdependencies of capabilities

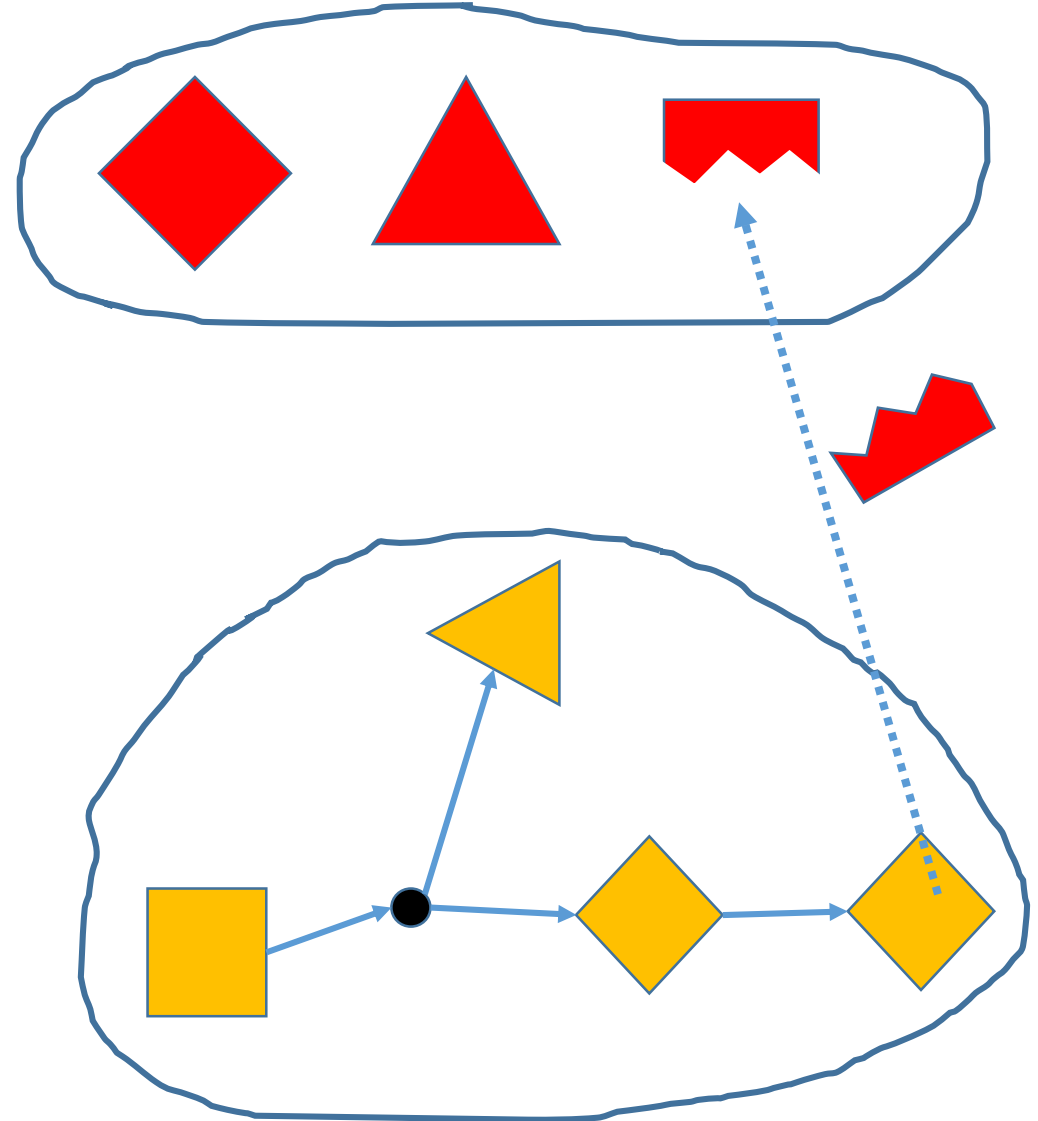
Step 5. List (systematically) confidential information

Step 6. Identify threats



Security Landscape

- Step 1. Define the interface
- Step 2. Determine “(ab)normal” outputs
- Step 3. List (systematically) adversary capabilities
- Step 4. Identify the interdependencies of capabilities
- Step 5. List (systematically) confidential information
- Step 6. Identify threats
- Step 7. Modify threats due to trivial attacks**



Step 1. Interface

Authenticated key establishment (AKE) protocols for 2 sides

Input:
Identifiers A, B

Output of A:
 S_A
 K_A
 R_A

Output of B:
 S_B
 K_B
 R_B

- *with whom?*
- *what?*
- *who is he?*

$\{B, P_B\}$, P_B is the partner
established key
the role of participant

Step 1. Interface

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- *with whom?*
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the role of participant

Protocol outputs:

$(S_A, K_A, R_A),$

(S_B, K_B, R_B)

Step 2. “(Ab)normal” outputs

Output properties

$$\begin{aligned} S_A &= S_B \\ K_A &= K_B \\ R_A &= R_B \end{aligned}$$

$$\begin{aligned} S_A &= S_B \\ K_A &= K_B \\ R_A &\neq R_B \end{aligned}$$

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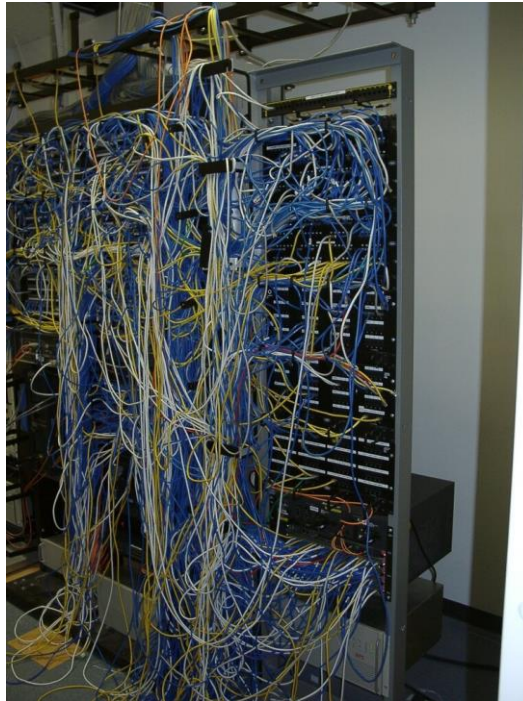
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Step 3. Adversary capabilities

26 adversary capabilities from 4 classes: C, UR, AR, UA

Channel (C)



Registration of users and the adversary (UR/AR)



User acting after registration (UA)

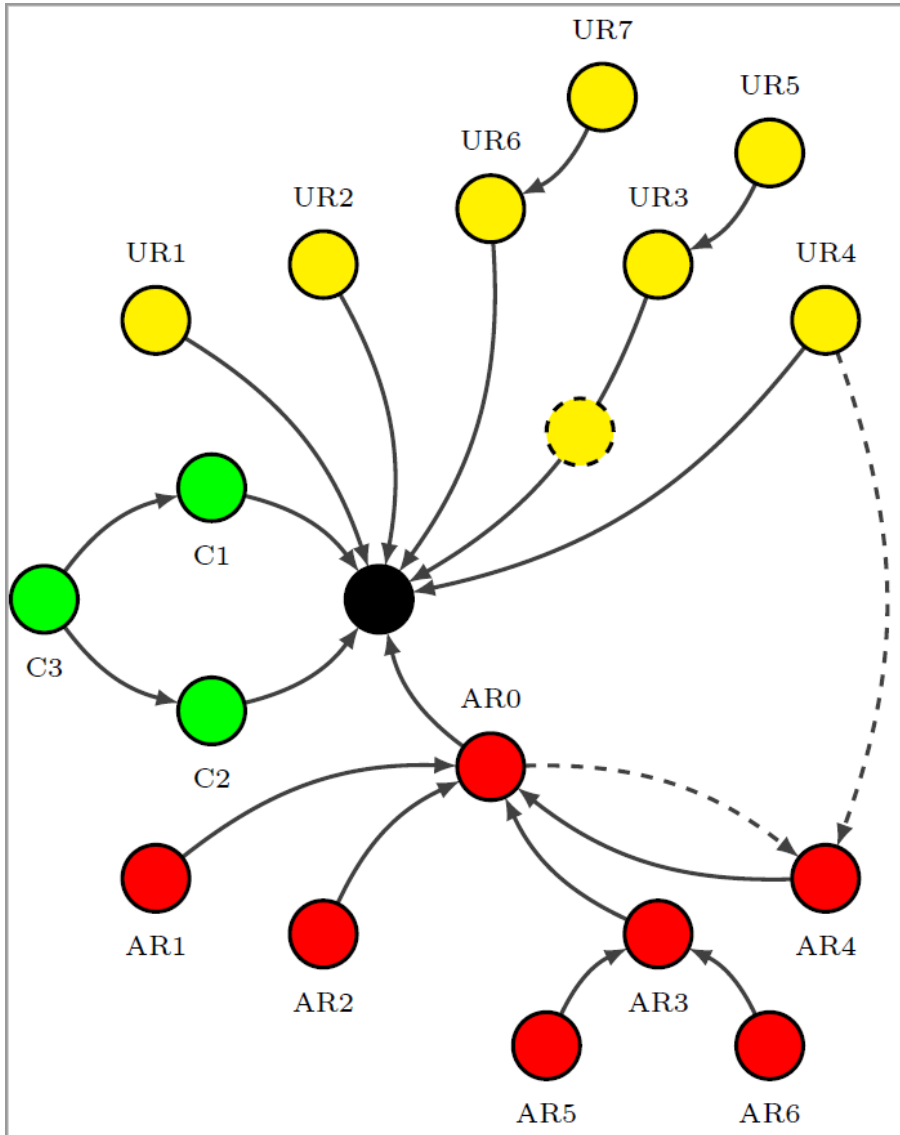


Step 3. Adversary capabilities

		Session key		Long-term key		Intermediate values	
		before session	after session	before session	after session	before session	after session
Key compromise	Secret	<i>no key</i>	✓	✓	✓	✓	✓
	Public	<i>no public key</i>		✓	✓	✓	✓

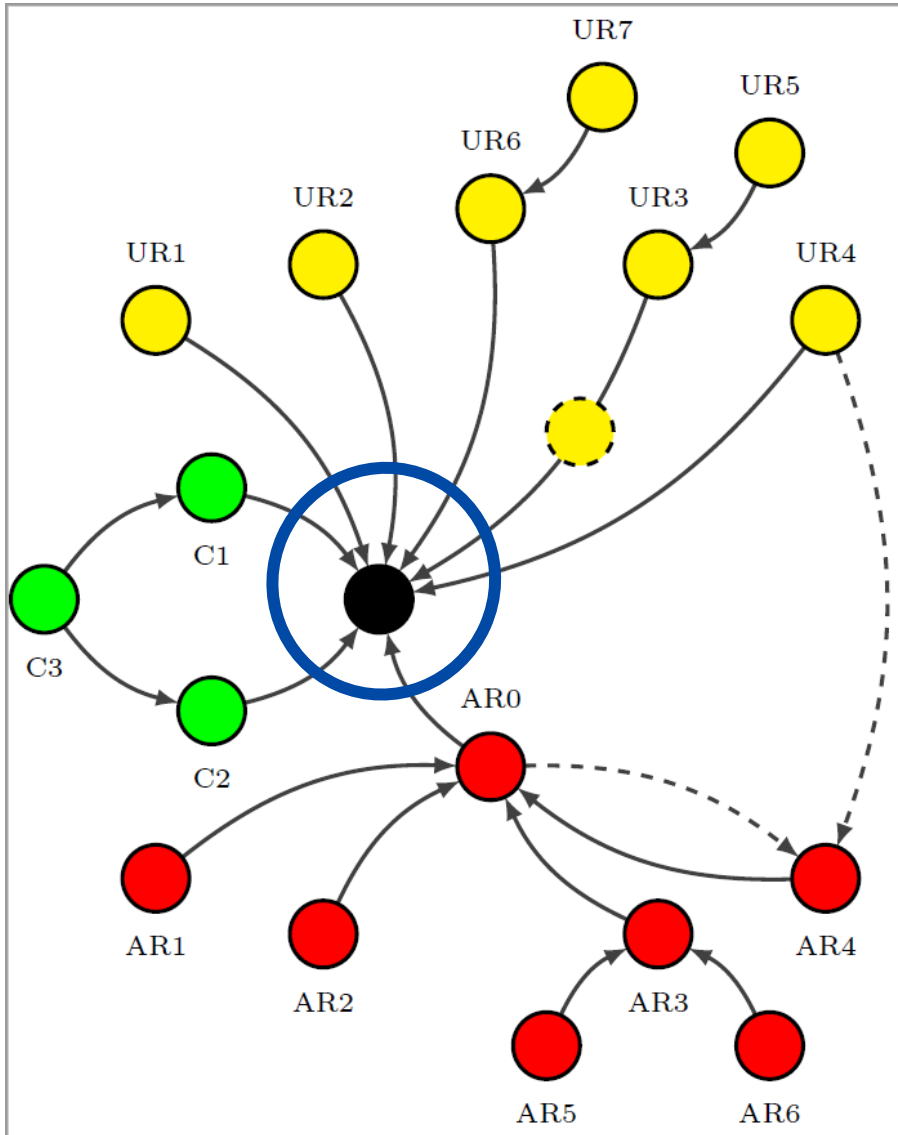
Key forcing and repeating		Long-term key		Intermediate values	
		Forcing	Repeating	Forcing	Repeating
Secret	✓	✓	✓	✓	
Public	✓	<i>no sense</i>	✓	✓	

Step 4. Interdependencies of capabilities



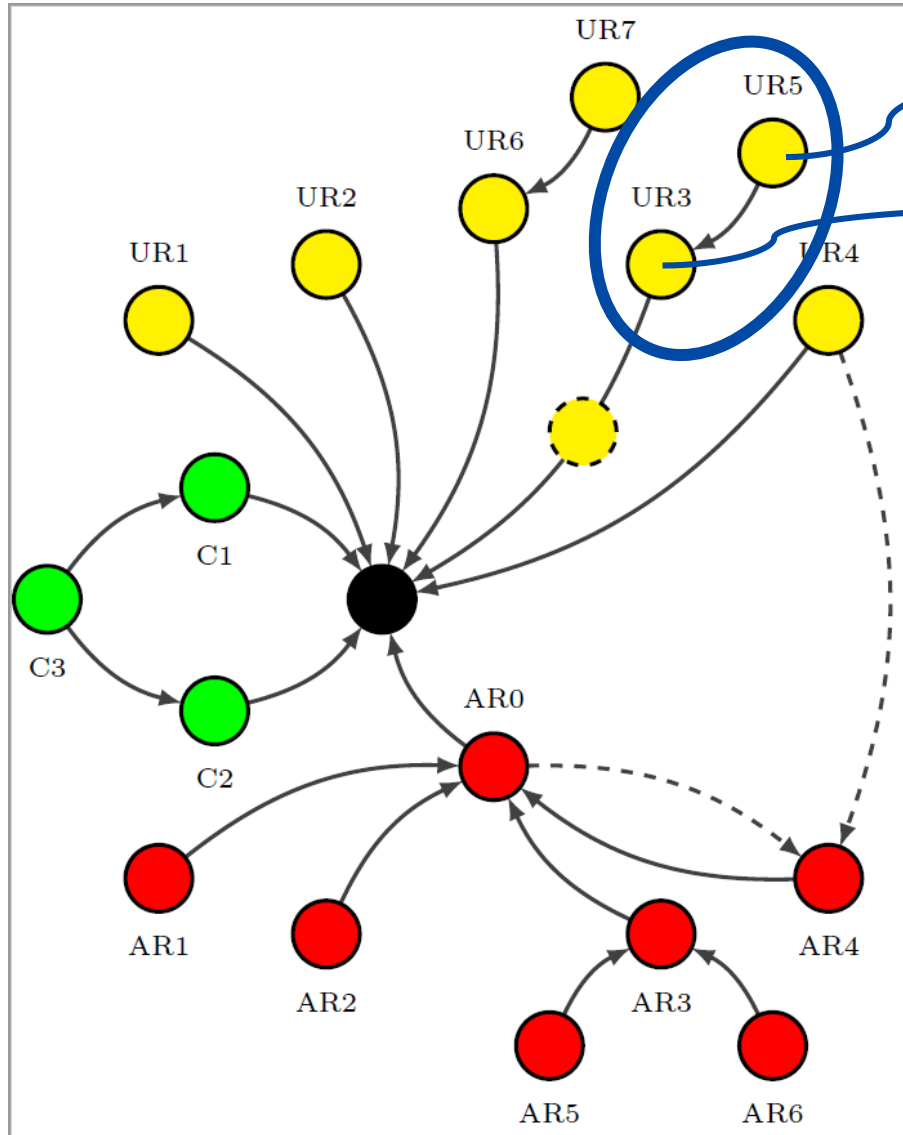
Adversary capabilities from classes C, AR, UR

Step 4. Interdependencies of capabilities



minimum adversary capabilities
(e.g. knowledge of public keys)

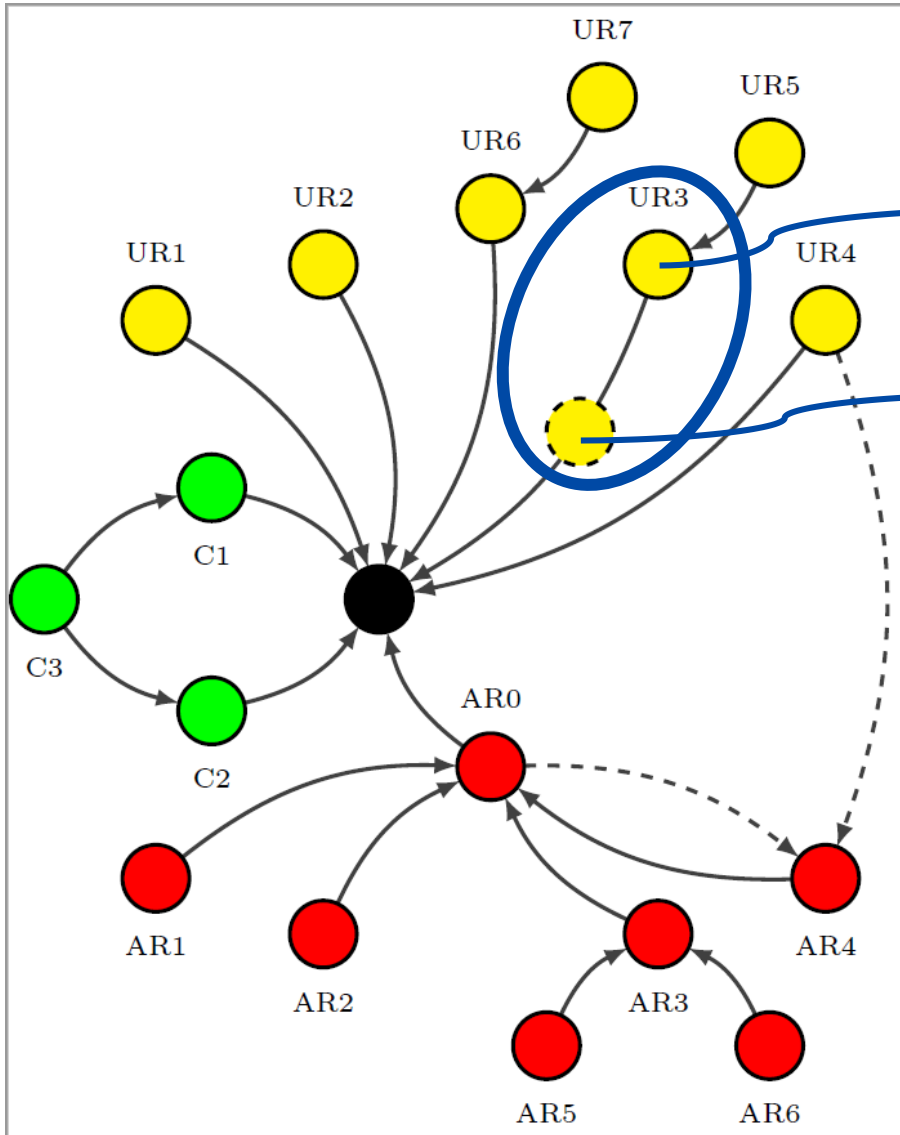
Step 4. Interdependencies of capabilities



Forcing inconsistent key

Forcing a key

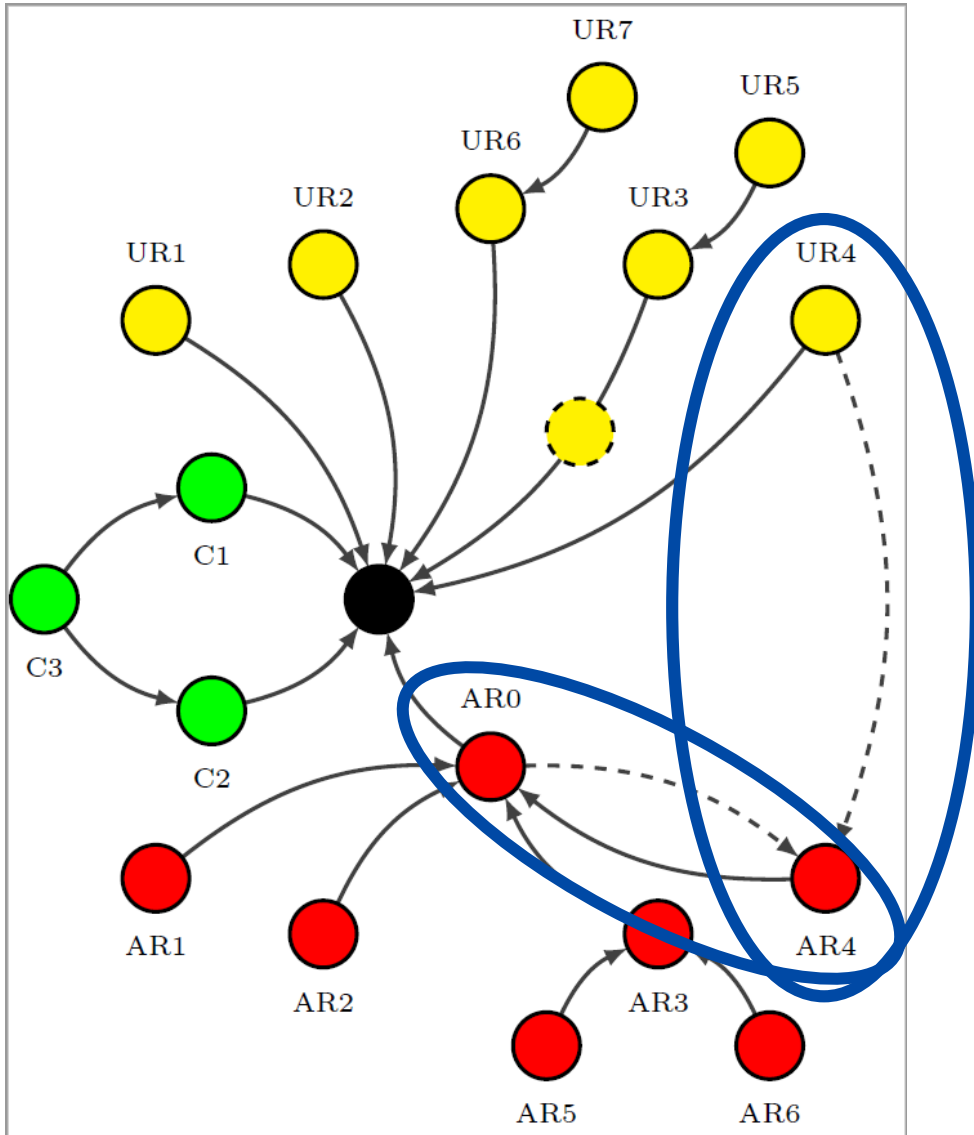
Step 4. Interdependencies of capabilities



Forcing a key

Forcing a key with some property

Step 4. Interdependencies of capabilities



the adversary has UR4 and AR0 capabilities
 \Rightarrow the adversary has the capability AR4

Step 5. Confidential information

Output of A:

S_A

K_A

R_A

Output of B:

S_B

K_B

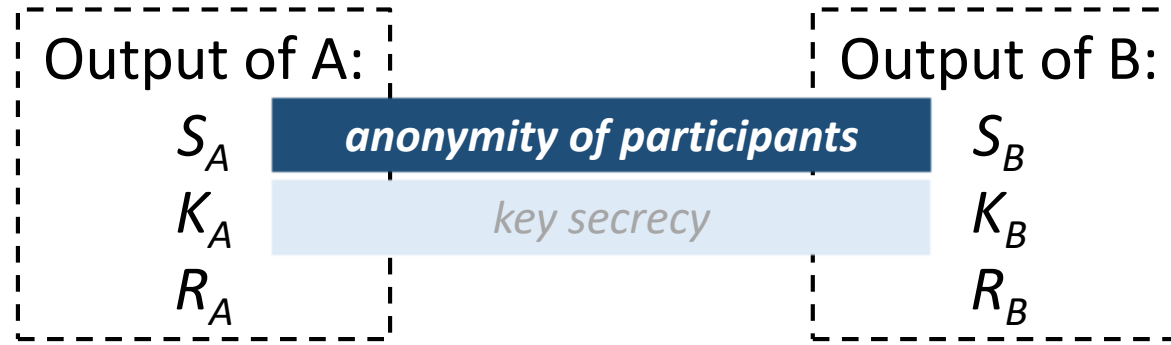
R_B

Step 5. Confidential information



K_A or/and K_B are distinguishable from random for anyone other than A, B

Step 5. Confidential information



P_A or/and P_B are distinguishable from random for anyone other than A, B

Step 5. Confidential information



R_A or/and R_B are distinguishable from random for anyone other than A, B

Step 6. Threats

Examples of security properties **for AKE protocols** [SN22]:

- **Message authentication** – confirmation of the authenticity of the message source and the integrity of the transmitted message
- **Replay protection** – once correctly accepted by the participant, the message should not be accepted again
- **Key secrecy** – during the interaction, the key cannot become known to the adversary, as well as to users for whom this key is not intended
- **Key authentication** – the participant **receives confirmation that no other participant, except the second one, can know the secret key generated during the protocol execution**

not the final security properties of AKE

appear to be the same

Step 6. Threats

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Authentication Disruption

Step 6. Threats

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Key Inequality

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Forcing Identical Roles (FIR) [AKS23]

Key Inequality

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Authentication Disruption

[AKS23] Alekseev E., Kyazhin S. & Smyshlyaev S. The threat of forcing the identical roles for authenticated key establishment protocols // J. Comput. Virol. Hack. Tech., 2023

Step 6. Threats

Authentication Disruption

$$S_A \neq S_B$$

$$K_A = K_B$$

$$R_A = R_B$$

$$S_A \neq S_B$$

$$K_A = K_B$$

$$R_A \neq R_B$$

$$S_A \neq S_B$$

$$K_A \neq K_B$$

$$R_A = R_B$$

$$S_A \neq S_B$$

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$$R_A \neq R_B$$

Step 6. Threats

Authentication Disruption

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$$S_A \neq S_B$$

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Unknown Key Share (UKS)

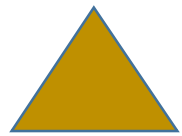
Step 6. Threats

Deniability:

the output of the protocol (together with its transcript) allows the user to prove participation in the protocol session

Deniability cannot be described using our systematization 😞

Step 7. Threats Modification

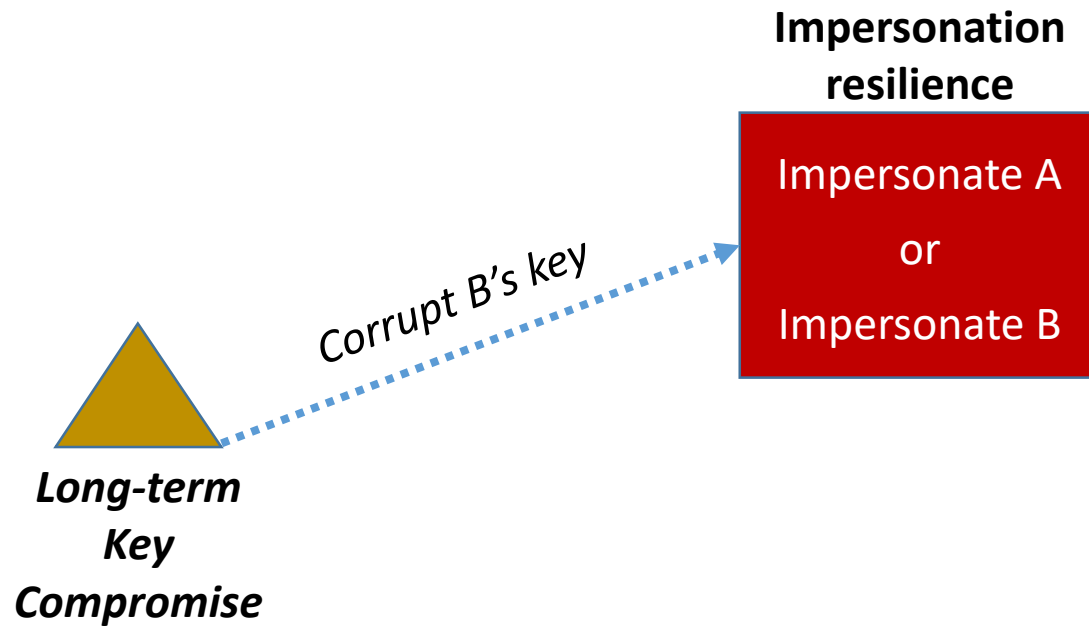


***Long-term
Key
Compromise***

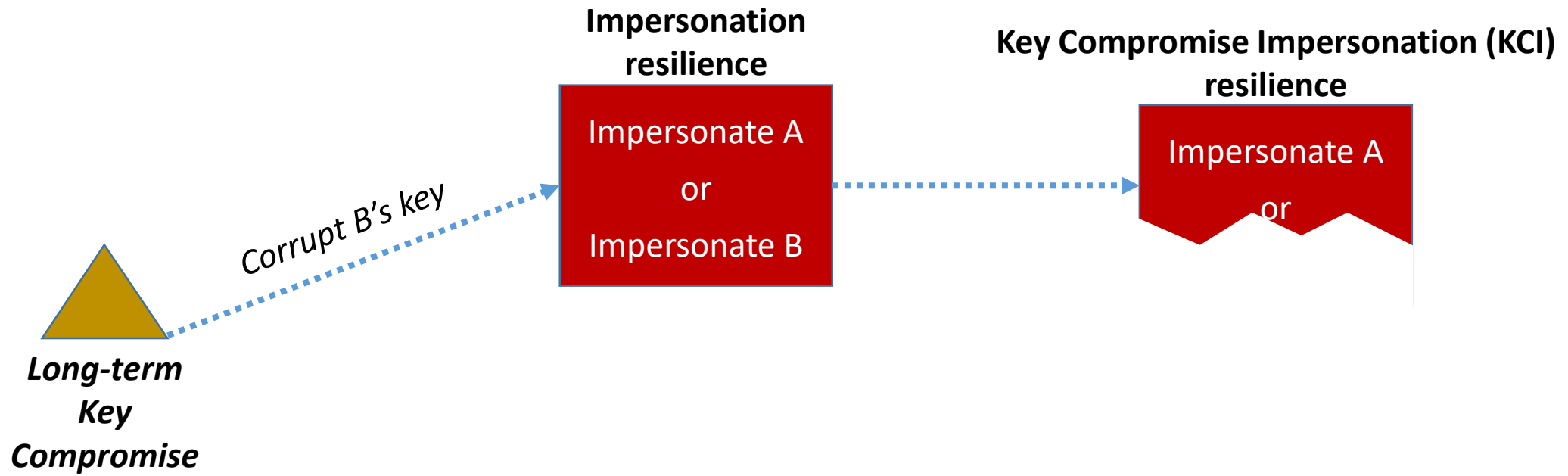
**Impersonation
resilience**

Impersonate A
or
Impersonate B

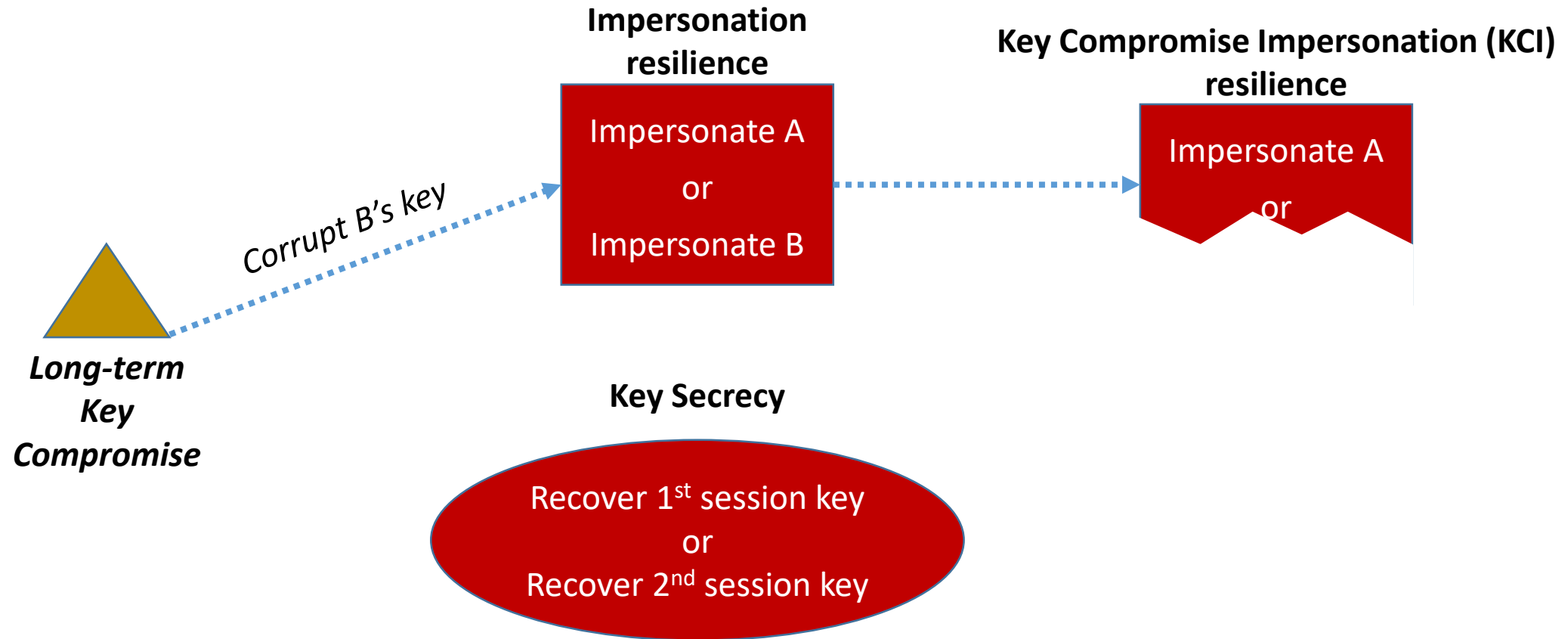
Step 7. Threats Modification



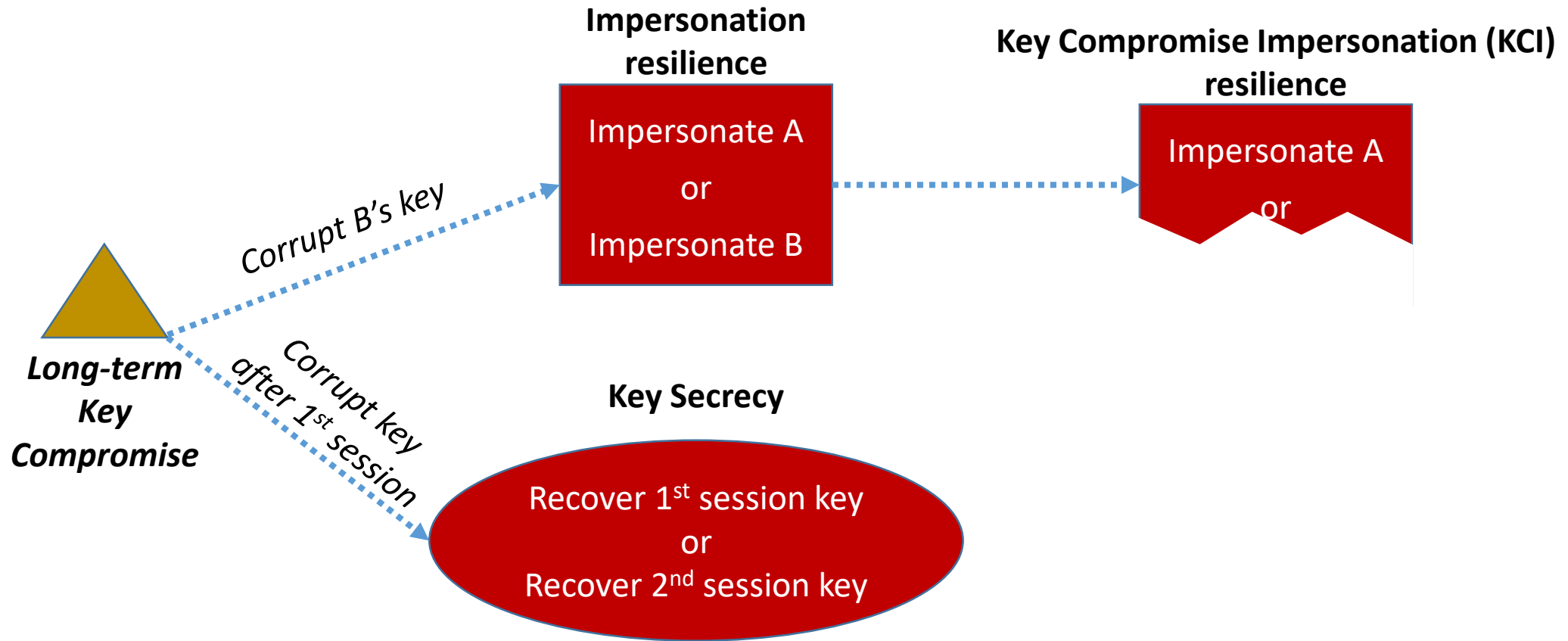
Step 7. Threats Modification



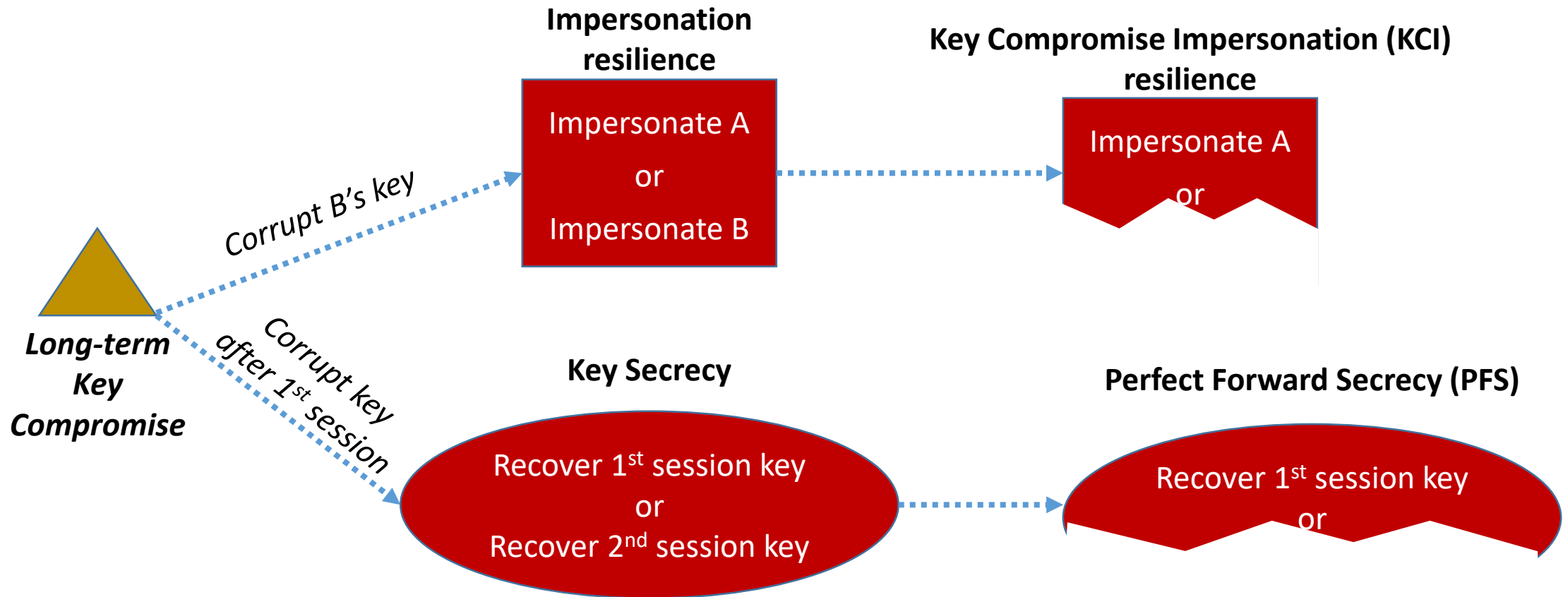
Step 7. Threats Modification



Step 7. Threats Modification



Step 7. Threats Modification



Additional Remarks

Seemingly independent threats can be interdependent...

Example of attack [DP18]: **KCI** \Rightarrow **PFS** disruption

May be it is necessary to add Step 8. Identify the interdependencies of threats

Interesting findings, or Conclusion

- The usual systematization of threats described in this paper is not complete (there are such security properties as deniability)
- There are subsets of AKE protocol outputs that can be considered as separate threats, but they were not previously classified as such (for example, a FIR threat)
- Seemingly independent threats can be interdependent

It is useful to form a security landscape, because otherwise something may not be taken into account (but it would be good to take everything into account)

Thank you for your attention!

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