

# An approach to the analysis of CryptoPro KeyMeshing

Anton Naumenko  
Yaroslavl, 2016



## Specification of CryptoPro Key Meshing

Let we have

$C = \{0x22720069L, 0x2304C964L, 0x96DB3A8DL, 0xC42AE946L, 0x94ACFE18L, 0x1207ED00L, 0xC2DC86C0L, 0x2BA94CEFL\}$ .

and a random key

$$K_0 \in \{0,1\}^{256}$$

Key Meshing is

$$K_{r+1}(K_0) = \text{Decrypt}_{K_r(K_0)}(C), r = 0, 1, \dots$$

### Basic properties of CryptoPro Key Meshing

For any  $r \geq 1$  and  $K_0$

$$K_r(K_0) \in B, B = \{(x_0//x_1//x_2//x_3); x_i \in \{0,1\}^{64}, x_i \neq x_j, i \neq j\}$$

Denote

$$B_r = \bigcup_{K_0} \{K_r(K_0)\}.$$

**Property 1**

$$B \supseteq B_1 \supseteq B_2 \supseteq \dots \supseteq B_r \supseteq B_{r+1} \supseteq \dots$$



# Main results

If we consider **CryptoPro Key Meshing** as *random mapping* then (see Odlyzko 1990, Mironkin 2014):

$$E(|B_r|) = (1 - \tau_r) |B|; \text{ where } \tau_1 = e^{-1}; \tau_{i+1} = e^{-1+\tau_i}.$$

## Proposition 1

$$1 - \tau_r = \frac{2}{r} + \frac{2}{3r^3} + O(r^{-4}).$$

## Note

Elements of the set  $B_r$  have different probabilities (in considering model)

Let  $\Psi_r$  - probability distribution on elements of key set  $B_r$ .

Denote Shannon entropy as  $H(\Psi_r)$ .

## Proposition 2

$$H(\Psi_r) \approx \log_2 |B| - 2 \cdot \ln 2 \cdot \log_2 r - C,$$

$$C = 1.61\dots$$



Thanks for Attention!

Questions?

