

WITHIN A FRIEND ZONE: HOW FAR CAN WE
PROCEED WITH DATA ENCRYPTION NOT
GETTING OUT

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LET'S MOVE TO

INTRODUCTION

PROBLEMS AND SOLUTIONS

CONCLUSIONS

BC AND EVOLUTION OF TASKS

SIMPLE EXAMPLE¹

- ▶ SIZE OF THE INTERNET DOUBLES EVERY 2 YEARS
- ▶ FOR THE BEGINNING OF 2016: APPROX. 7.7 ZETTABYTE
- ▶ IN 2020: APPROX. 40 ZETTABYTE
- ▶ IN 2020: APPROX. 50 BILLION DEVICES WILL BE CONNECTED TO THE INTERNET

OLD NEW TASKS

- ▶ CONFIDENTIALITY,
- ▶ INTEGRITY,
- ▶ AUTHENTICATION,
- ▶ DIFFERENT COMBINATIONS OF TASKS.

SIMPLE SOLUTION: FROM BC TO BC MODES OF OPERATIONS

¹ACCORDING TO <http://live-counter.com>

BC AND MODES OF OPERATIONS

FROM ATTACKS ON BC TO ATTACKS ON MODES
FROM ATTACKS ON PRIMITIVES TO ATTACKS ON PROTOCOLS

RANGE OF TASKS \mapsto

RANGE OF ADVERSARY'S CAPABILITIES \mapsto

DIFFERENT ADVERSARIAL MODELS

EXAMPLE OF MODELS

- ▶ SIMPLE ANALYSIS,
- ▶ DISTINGUISHING ATTACKS,
- ▶ CROSS-MODES ATTACKS,
- ▶ FAULT ANALYSIS,
- ▶ MANY MORE OTHERS, SOME UNDISCOVERED AT THE MOMENT

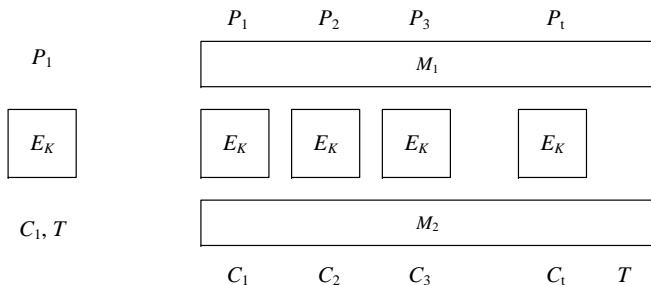
BC IN MODES AND EVOLUTION OF CRYPTANALYSIS

SIMPLE EXAMPLE

SWEET32: THEORETICAL ATTACK ON BC TO PRACTICAL ATTACK ON REAL-LIFE INFORMATIONAL SYSTEMS

CLEAR NEED:

- ▶ USE CASES FOR BC AND MODES OF OPERATIONS,
- ▶ LIMITATIONS ON USE OF BC AND MODES OF OPERATIONS,
- ▶ BASED ON USE CASES LIMITATIONS AND RESTRICTIONS FOR USE OF BC AND MODES OF OPERATIONS.



BC IN MODES VS. ADVERSARIES

TRIVIAL CONCLUSION

EACH CRYPTO MECHANISM COULD BE USED IN SUCH A WAY IT
COULD NOT PROVIDE SUFFICIENT² LEVEL OF SECURITY
OPPOS.: EACH CRYPTO MECHANISMS COULD BE PROVIDED WITH
LIMITATIONS IN A WAY IT WILL PROVIDE SUFFICIENT LEVEL
OF SECURITY

²FOR SOME USE CASES

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OBSERVATION NOTES

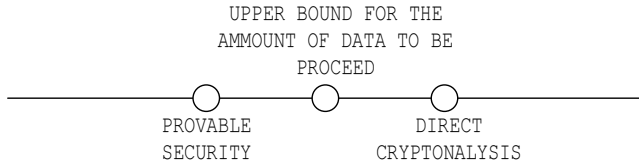
- ▶ BROAD STUDY OF MODES OF OPERATIONS,
- ▶ PROVABLE SECURITY APPROACH,
- ▶ DIRECT CRYPTANALYSIS APPROACH.

DIRECT CRYPTANALYSIS

THIS AMOUNT = ATTACK = UPPER VALUE FOR THE UPPER BOUND

PROVABLE SECURITY

MORE THEN THIS AMOUNT = ATTACK = LOWER VALUE FOR THE
UPPER BOUND



DIRECT ANALYSIS

- ▶ $P_1, P_2, \dots, P_u, P'_1, P'_2, \dots, P'_v$ - PLAINTEXT BLOCKS,
- ▶ $C_1, C_2, \dots, C_u, C'_1, C'_2, \dots, C'_v$ - CORRESPONDING CIPHER-TEXT BLOCKS.

DIRECT ANALYSIS

- ▶ $P_1, P_2, \dots, P_u, P'_1, P'_2, \dots, P'_v$ - PLAINTEXT BLOCKS,
- ▶ $C_1, C_2, \dots, C_u, C'_1, C'_2, \dots, C'_v$ - CORRESPONDING CIPHER-TEXT BLOCKS.

TASK: OBTAIN ADDITIONAL INFORMATION ABOUT UNKNOWN PART OF THE PLAINTEXT WITH PROBABILITY NO LESS THEN π .




SOME OBSERVATIONS:



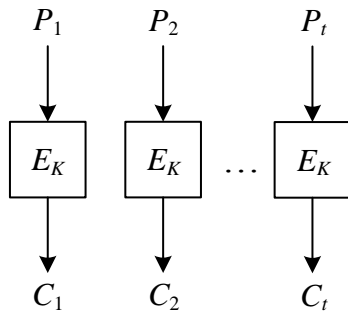
McGrew, D. IMPOSSIBLE PLAINTEXT CRYPTANALYSIS AND PROBABLE-PLAINTEXT COLLISION ATTACKS OF 64-BIT BLOCK CIPHER MODES.

PROVABLE SECURITY

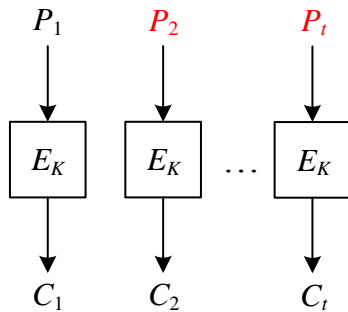
SOME USEFUL RESULTS:

-  ROGAWAY, P. EVALUATION OF SOME BLOCKCIPHER MODES OF OPERATION.
 -  BELLARE, M., DESAI, A., JOKIPIII, E., AND ROGAWAY, P. A CONCRETE SECURITY TREATMENT OF SYMMETRIC ENCRYPTION.
 -  A. ALKASSAR, A. GERALDY, B. PFITZMANN, A.-R. SADEGHI. OPTIMIZED SELF-SYNCHRONIZING MODE OF OPERATION.
-
- ▶ LEFT-OR-RIGHT DISTINGUISHER,
 - ▶ TIME OF WORK t ,
 - ▶ q QUERIES [OF THE TOTAL LENGTH μ] TO SOME ORACLE,
 - ▶ BIRTHDAY PARADOX.

ECB



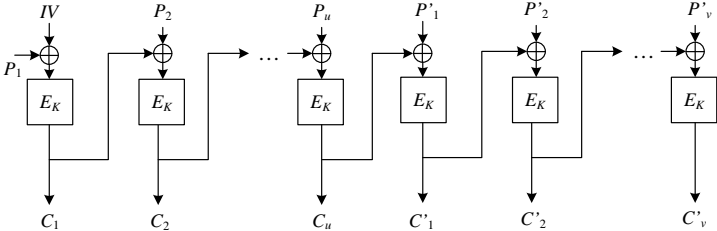
ECB



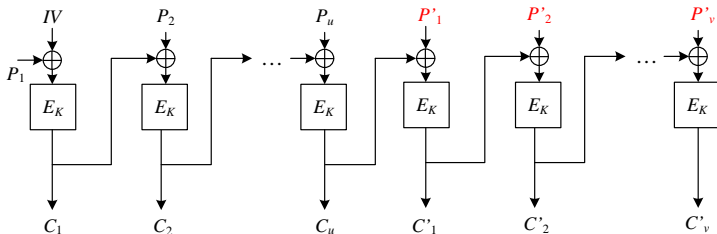
COMPLEXITY OF BRUTEFORCE ATTACK:

FROM 2^{tn} TO $2^n(2^n - 1) \dots (2^n - t + 1)$.

CBC



CBC



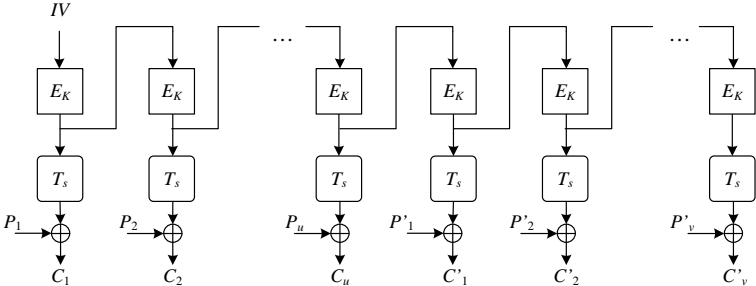
ASSUME $C_i = C'_j$. $P_i = D_K(C_i) \oplus C_{i-1}$, $P'_j = D_K(C'_j) \oplus C'_{j-1}$
THEN

$$P'_j = P_i \oplus C_{i-1} \oplus C'_{j-1}.$$

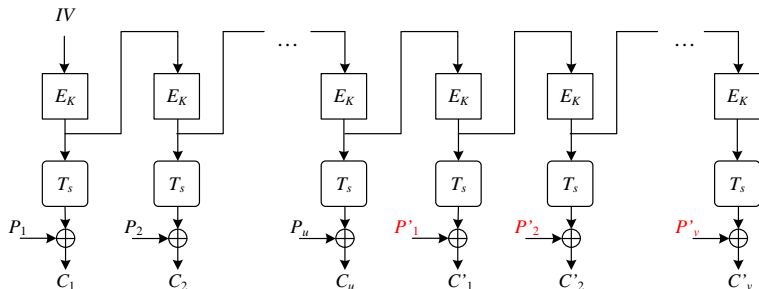
PROVABLE SECURITY PERSPECTIVE:

$$\Delta_{\text{CBC}_{\mathcal{F}}}^{lr}(t, q, \mu) \leq \frac{1}{2^{n-1}} \cdot q^2 + \frac{1}{2^n} \cdot q.$$

OFB



OFB



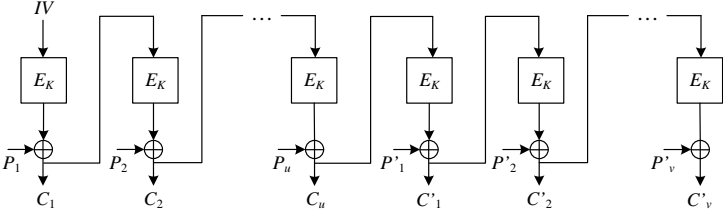
$P_i = E_K^i(a) \oplus C_i$, $P'_j = E_K^{j+u}(a) \oplus C'_j$, THEN IT IS POSSIBLE THAT $E_K^i(a) = E_K^{j+u}(a)$ AND

$$P'_j = P_i \oplus C_i \oplus C'_j.$$

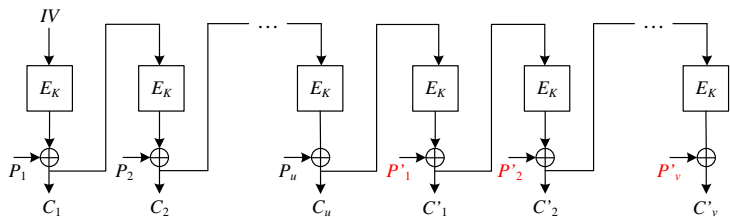
PROVABLE SECURITY PERSPECTIVE:

$$\Delta_{\text{OFB}_{\mathcal{F}}}^{lr}(t, q, \mu) \leq \frac{1}{2^{n-1}} \cdot q^2 + \frac{1}{2^n} \cdot q.$$

CFB



CFB



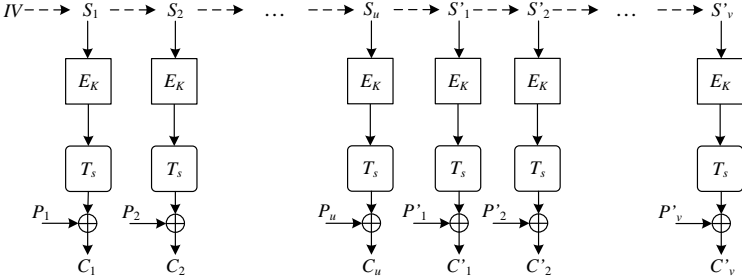
ASSUME C_{i-1} AND C'_{j-1} . $P_i = E_K(C_{i-1}) \oplus C_i$, $P'_j = E_K(C'_{j-1}) \oplus C'_j$ THEN

$$P'_j = P_i \oplus C_i \oplus C'_j,$$

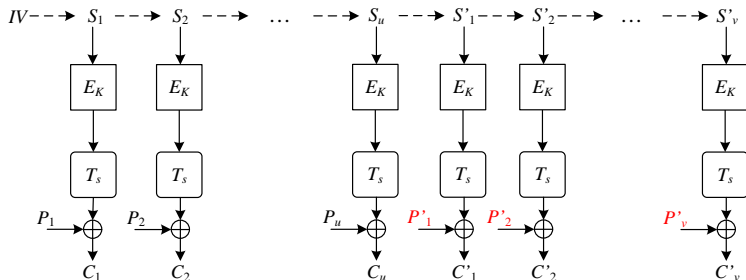
PROVABLE SECURITY PERSPECTIVE:

$$\Delta_{\text{CFB}_{\mathcal{F}}}^{lr}(t, q, \mu) \leq \frac{q^2}{2^n} + \frac{q(q-1)}{2^{n+1}}.$$

CTR



CTR



ALL VALUES $P_i \oplus C_i$ AND $P' \oplus C'_j$ ARE PAIRWISE DISTINCT.
THEN UNKNOWN PLAINTEXT BLOCK CAN 'T BELONG TO THE SET
 $M = \{P_i \oplus C_i \oplus C'_j \mid i \in \overline{1, u}, j \in \overline{1, v}\}$.

PROVABLE SECURITY PERSPECTIVE:

$$\Delta_{\text{CTR}\$_{\mathcal{F}}}^{lr}(t, q, \mu) \leq \frac{q^2}{2^n} + \frac{\mu(q-1)}{n \cdot 2^n}, \quad \Delta_{\text{CTR}\mathcal{C}_{\mathcal{F}}}^{lr}(t, q, \mu) \leq \frac{q^2}{2^n}.$$

SUMMARY

TABLE: UPPER BOUNDS FOR ACCEPTABLE AMOUNT OF DATA TO BE PROCESSED.

MODE OF OPERATION	MARGIN 1	MARGIN 2
ECB	1	-
CTR	$2^{\frac{n}{2}+1} \sqrt{\ln(\pi 2^n)}$	$\sqrt{\varepsilon} \cdot 2^{\frac{n}{2}}$
OFB	$2^{\frac{n}{2}} \sqrt{\ln\left(\frac{1}{1-\pi}\right)}$	$\sqrt{\varepsilon} \cdot 2^{\frac{n-1}{2}}$
CBC	$2^{\frac{n}{2}+1} \sqrt{\ln\left(\frac{1}{1-\pi}\right)}$	$\sqrt{\varepsilon} \cdot 2^{\frac{n-1}{2}}$
CFB	$2^{\frac{n}{2}+1} \sqrt{\ln\left(\frac{1}{1-\pi}\right)}$	$\sqrt{\varepsilon} \cdot \frac{1}{\sqrt{3}} 2^{\frac{n+1}{2}}$

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CONCLUSIONS

- ▶ DIFFERENT TASKS - DIFFERENT MODES,
- ▶ DIFFERENT TASKS - DIFFERENT ADVERSARIES,
- ▶ LIMITATION AND RESTRICTIONS COULD BE PROVIDED,
- ▶ MAXIMUM ACCEPTABLE AMOUNT OF BLOCKS TO BE PROCESSED WITHOUT KEY CHANGE ARE GIVEN,
- ▶ BOUNDARIES PRESENTED ARE VERY CLOSE, SO, AMOUNT OF DATA CAN BE SET.
- ▶ NOT UNIVERSAL RESTRICTIONS, JUST THE MOST WEAK ONES.

THANK YOU FOR YOUR ATTENTION!

ANY QUESTIONS?

FEEL FREE TO CONTACT US ON ANY MATTER AT

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